PatchGuard: A Provably Robust Defense against Adversarial Patches via Small Receptive Fields and Masking

Chong Xiang⁺, Arjun Nitin Bhagoji[‡], Vikash Sehwag⁺, Prateek Mittal⁺ [†]Princeton University [‡]University of Chicago *USENIX Security Symposium 2021*

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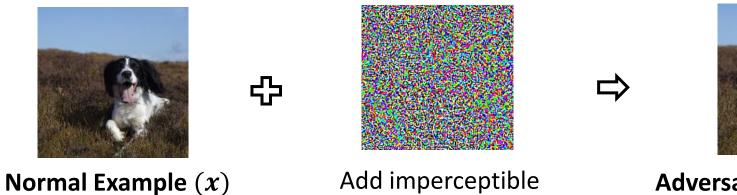
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PatchGuard: A Provably Robust Defense against Adversarial

Patches via Small Receptive Fields and Masking

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Adversarial Example Attacks: Small Perturbations for Test-Time Model Misclassification



Adversarial Example $(x + \delta)$ Cat (y')

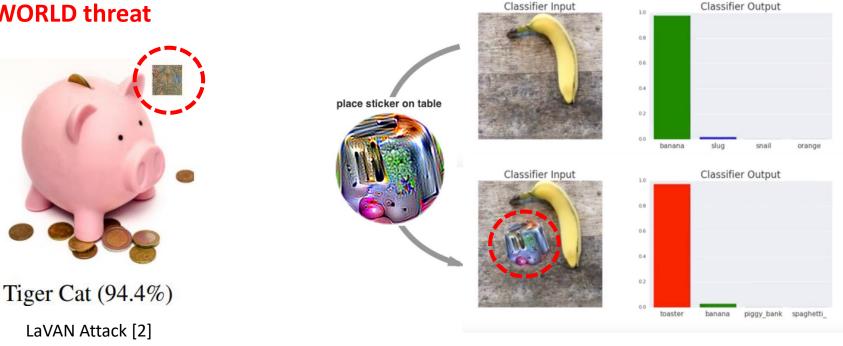
Dog (y) perturbations δ max $L(M(r + \delta))$

 $\max_{\delta} L(M(x + \delta), y)$ L(·)- Loss function; $M(\cdot)$ - Model

A threat to ML models! Challenge: Requires global perturbations

Our Focus: Localized Adversarial Patch Attacks

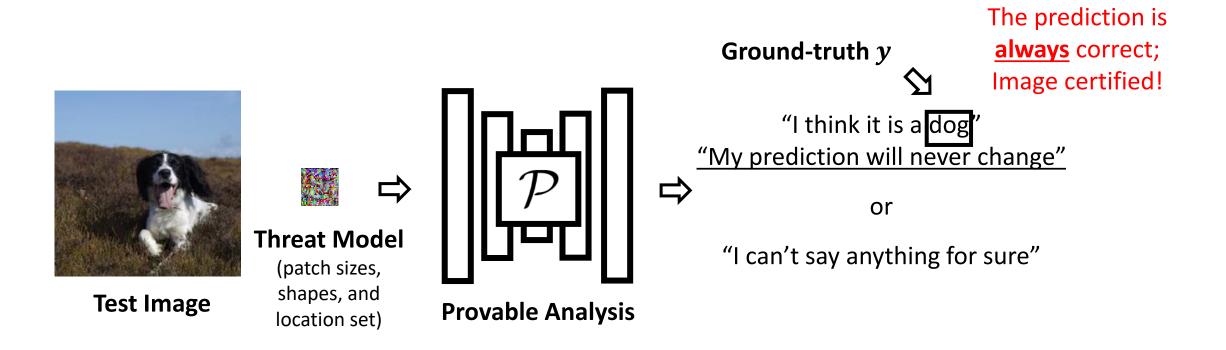
- 1. All perturbations within one local region (patch)
- 2. Patch pixels can take arbitrary values
- 3. Realizable in the physical world print and attach the patch!
 - A REAL-WORLD threat



Adversarial Patch [1]

- 4. Patch can be *anywhere* on the image
- 5. Patch size should be reasonable (shouldn't block the entire salient object)

Defense Objective: Provable Robustness on Certified Test Images

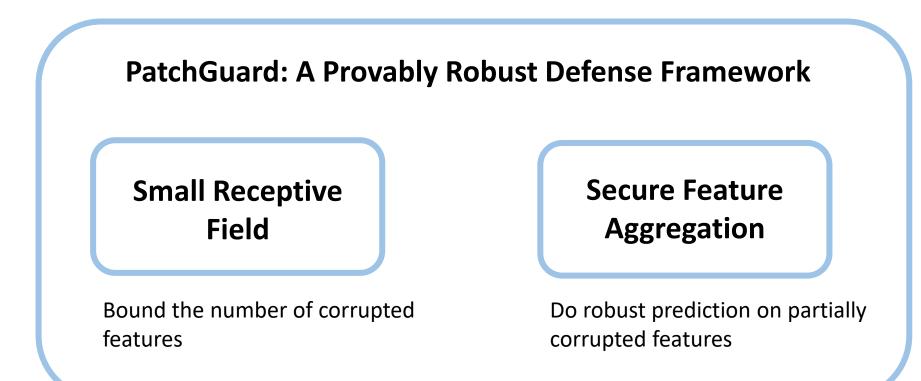


Provable robust accuracy / certified accuracy: the fraction of test images that are

- 1. Correctly classified
- 2. <u>Provably robust</u> to any (adaptive) localized patch attack within the threat model

Our Contribution: PatchGuard Defense Framework with Provable Robustness

PatchGuard aims to prevent the localized patch from dominating the global prediction

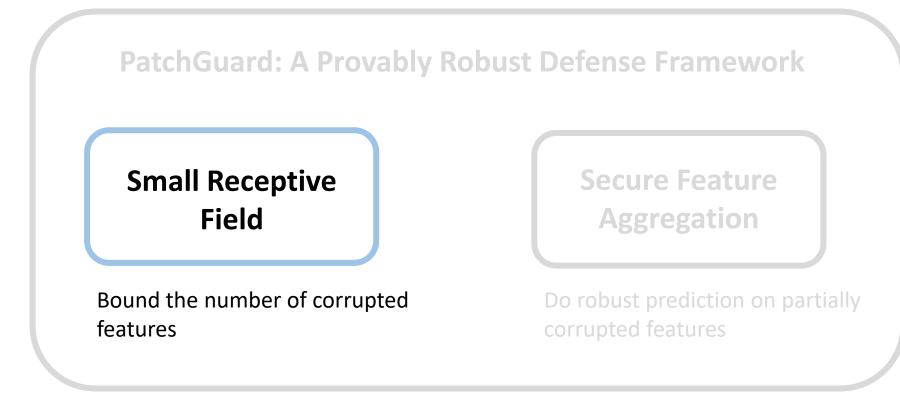




Tiger Cat (94.4%)

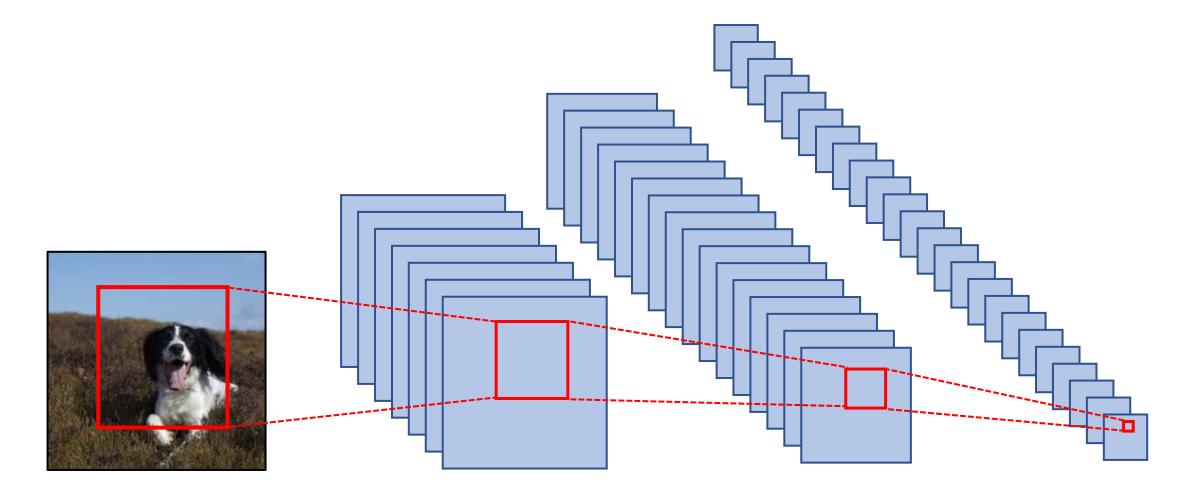
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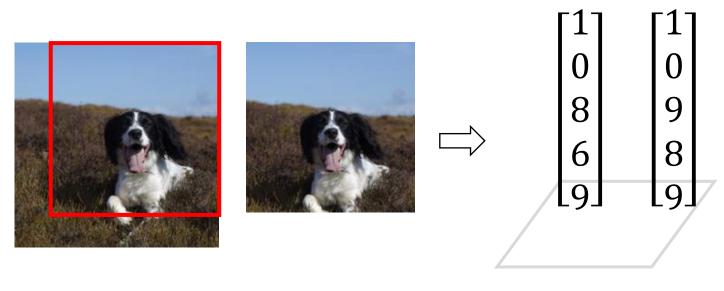


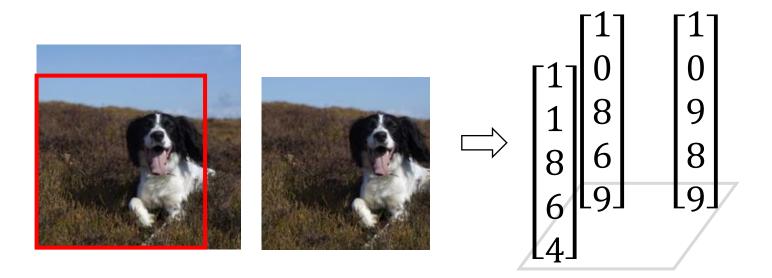


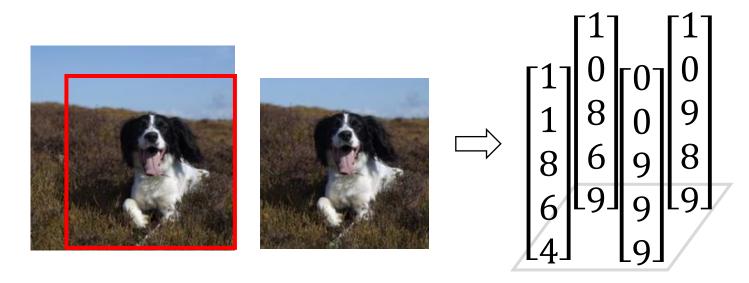
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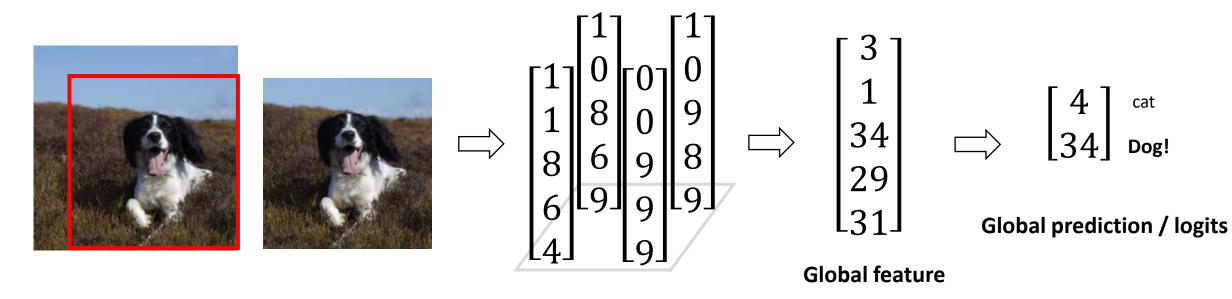




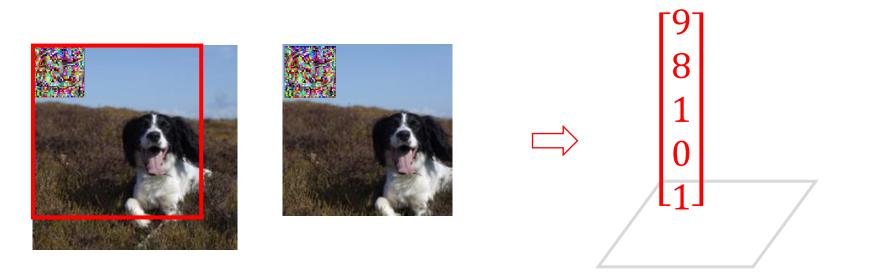




Aggregate Local Features for Global Prediction



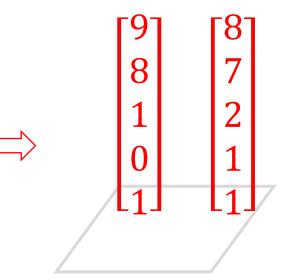
Example 1: CNN with *large* receptive fields (e.g., ResNet with 483×483 px)



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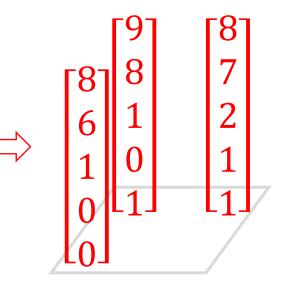




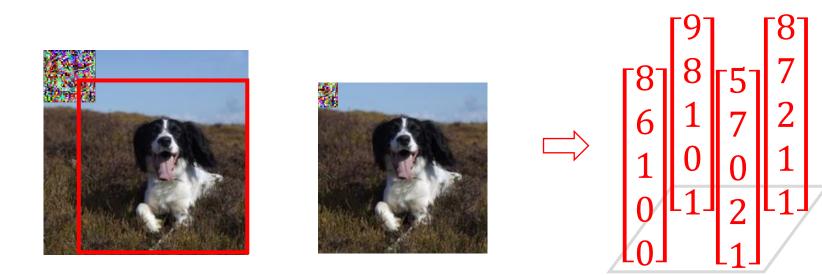
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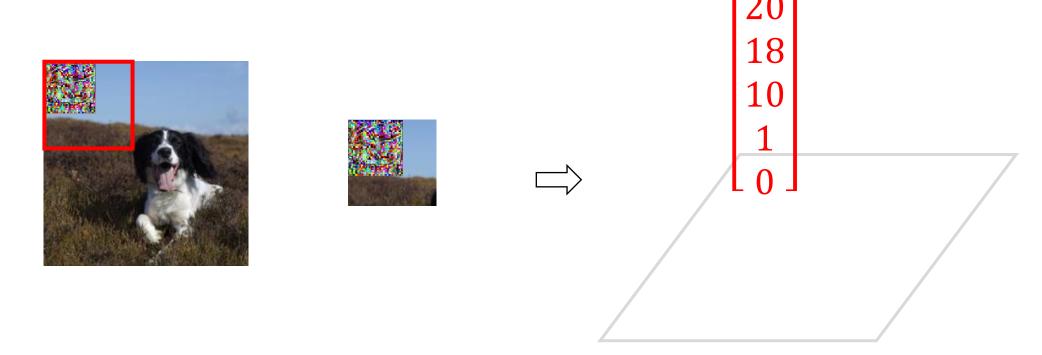


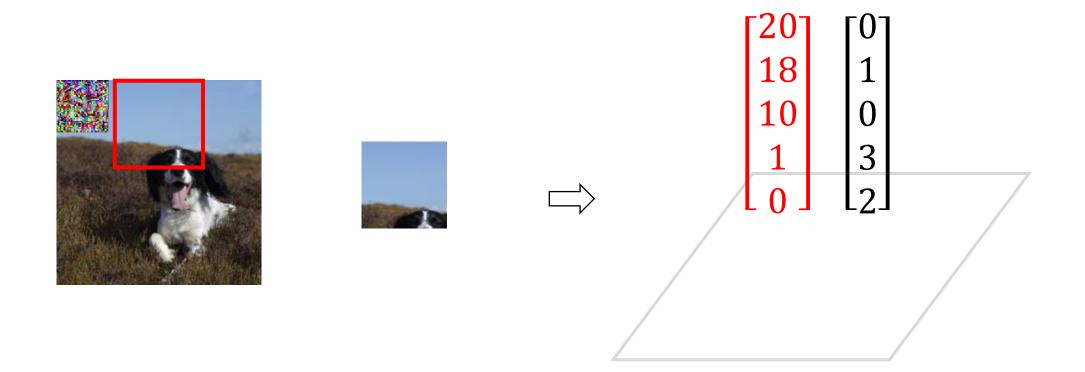
Example 1: CNN with *large* receptive fields (e.g., ResNet with 483×483 px)



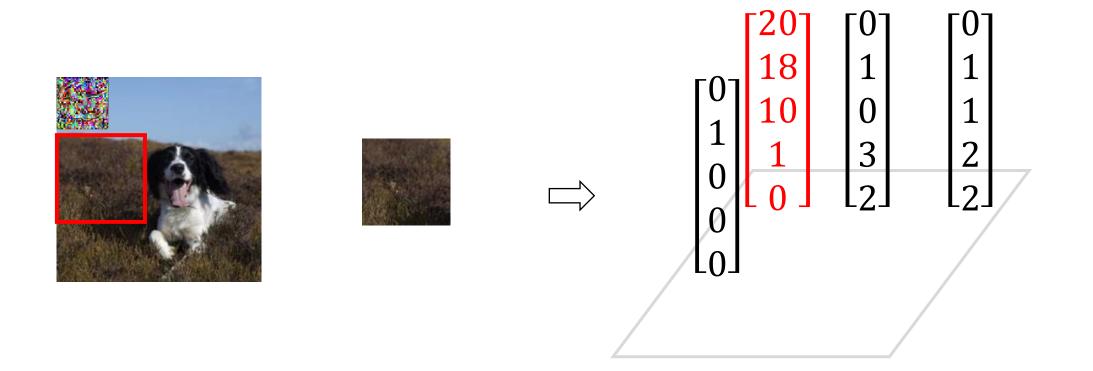
Local feature map

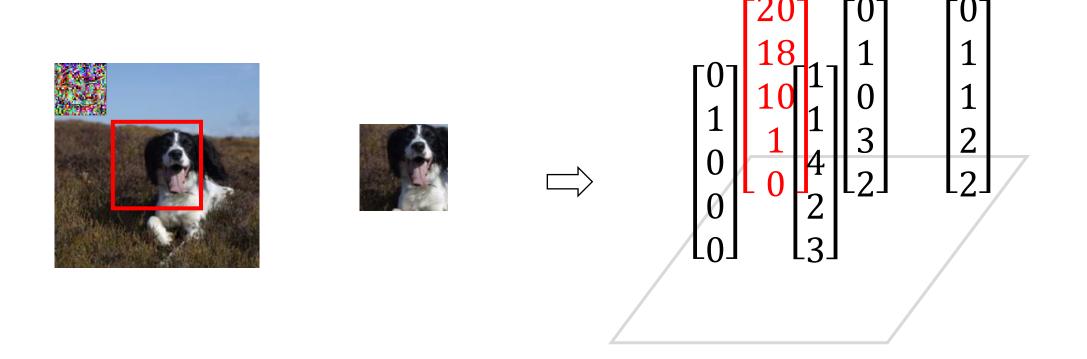
Note: *all* feature corrupted! Little hope for us to do a robust prediction





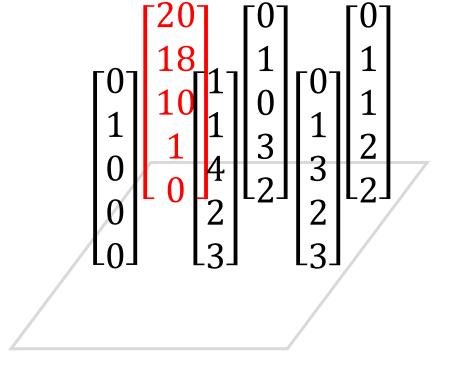






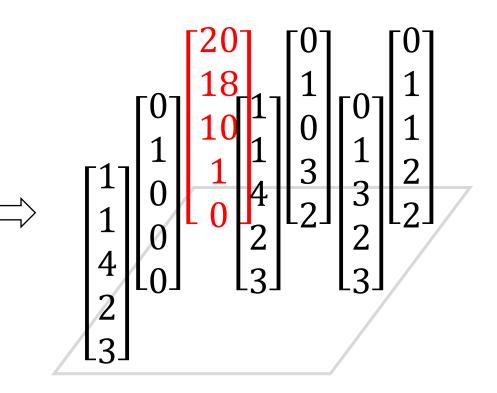






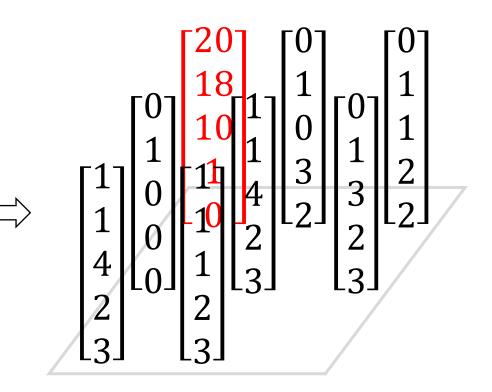










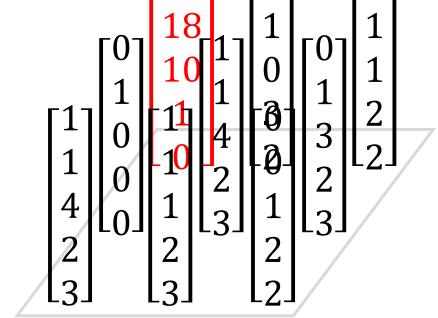


Example 2: CNN with *small* receptive fields (e.g., BagNet with 17×17 px)









Note: *only one* feature corrupted! A major step towards robust prediction!

Number of corrupted features k (along one axis) satisfies:

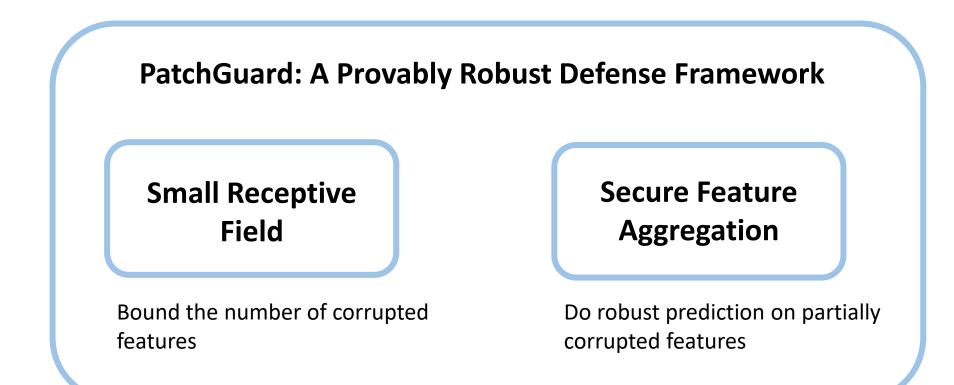
$$k = \frac{p+r-1}{s}$$

p patch size; r receptive field size; s receptive field stride (more details are in the paper)

A smaller receptive field gives fewer corrupted features!

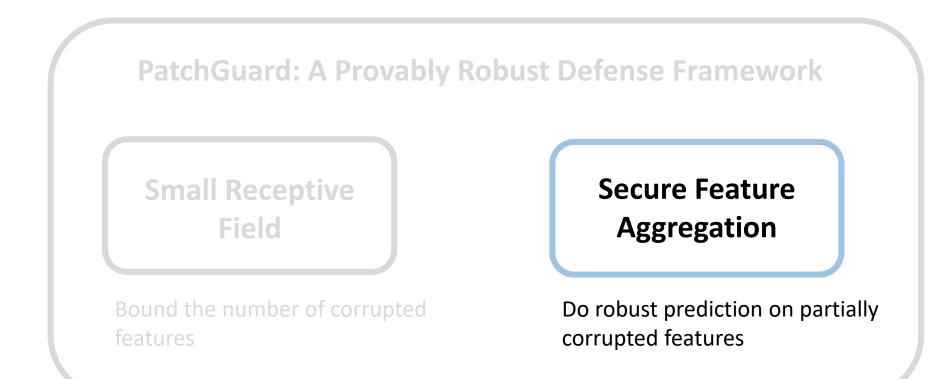
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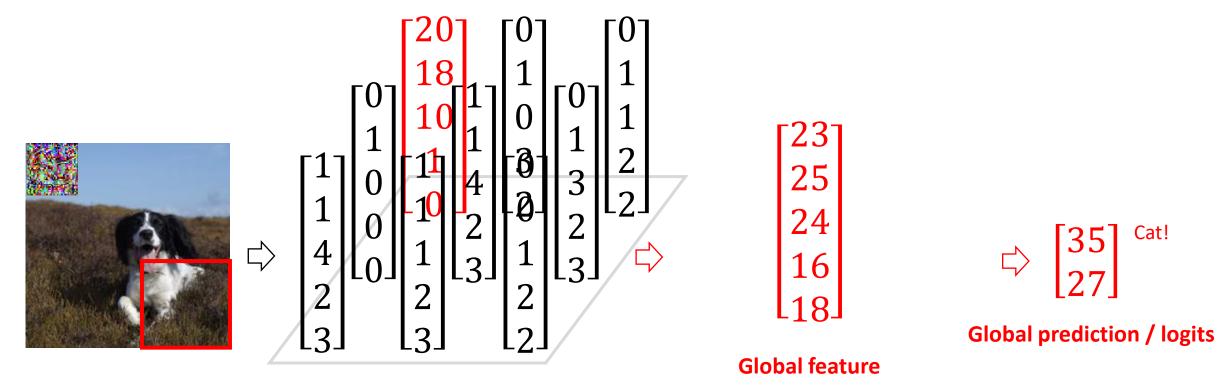
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Vulnerability of Insecure Feature Aggregation

Extremely large malicious values dominate the insecure feature aggregation and global prediction

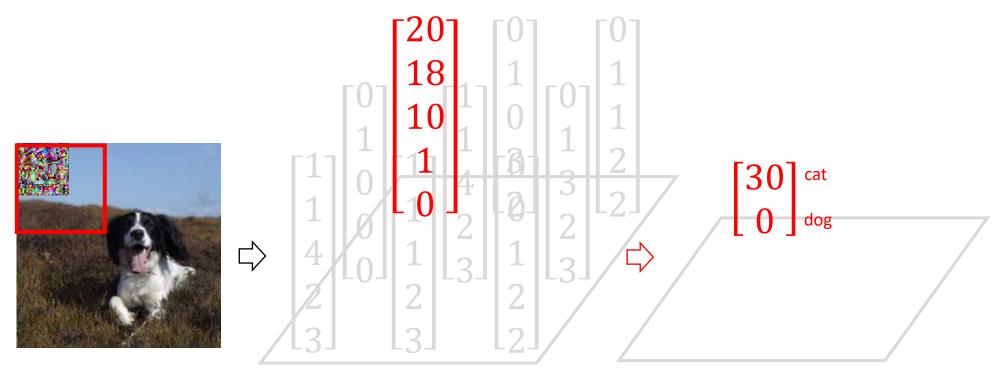


Local feature map

Secure feature aggregation to limit the adversarial effect!

• Robust masking to detect and remove large values

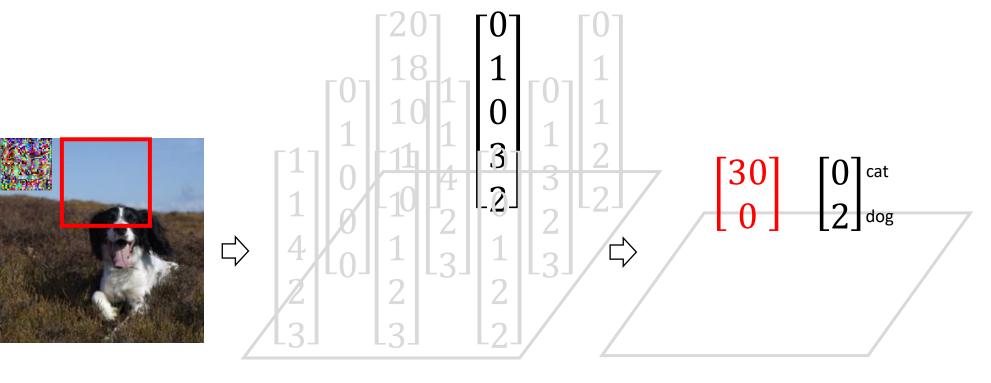
Local logits: making local prediction based on the local feature



Local feature map

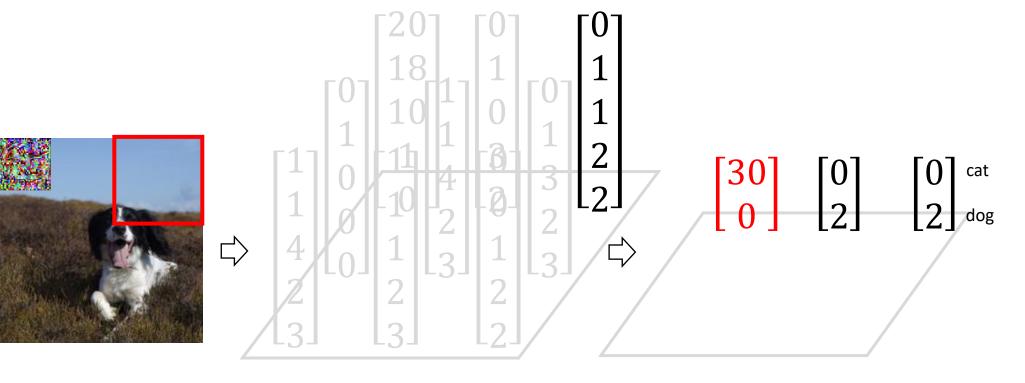
Local prediction / logits map

Local logits: making local prediction based on the local feature



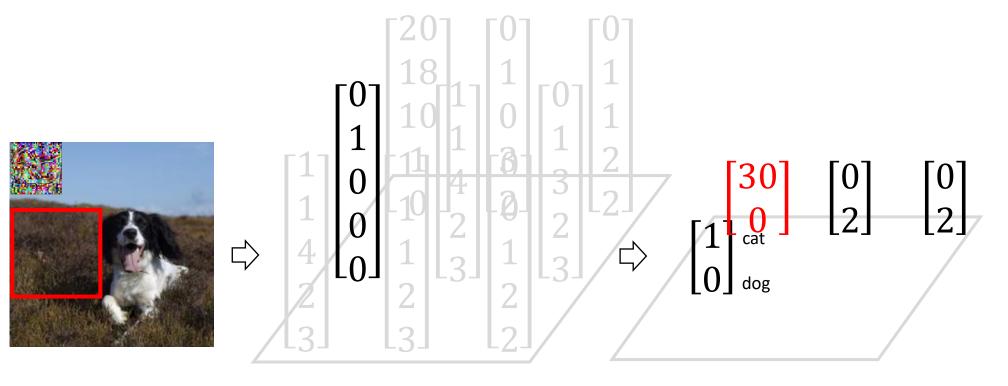
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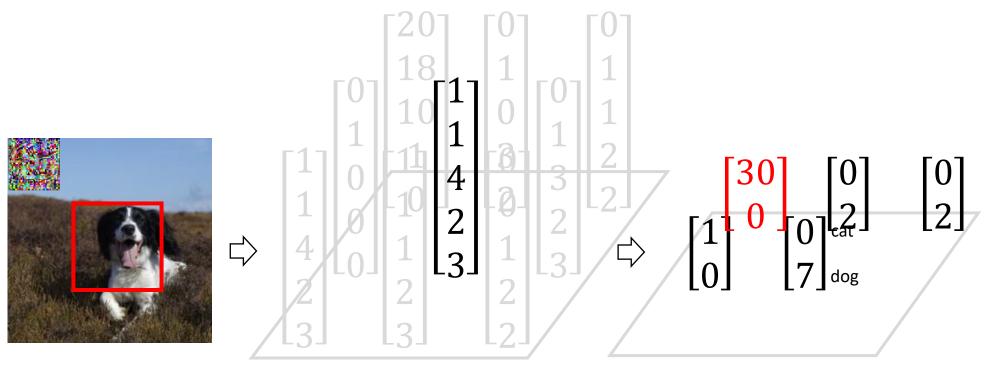
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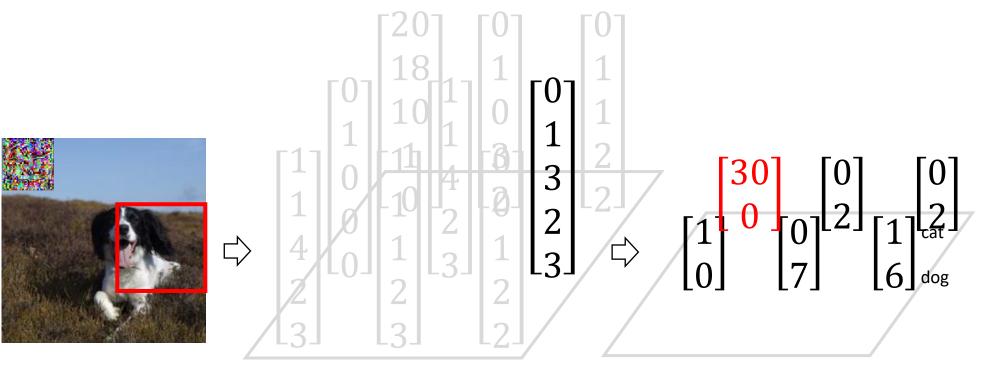
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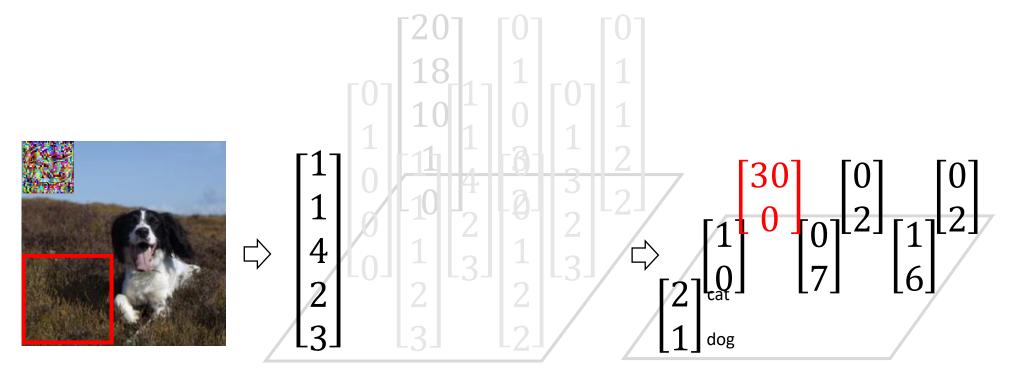
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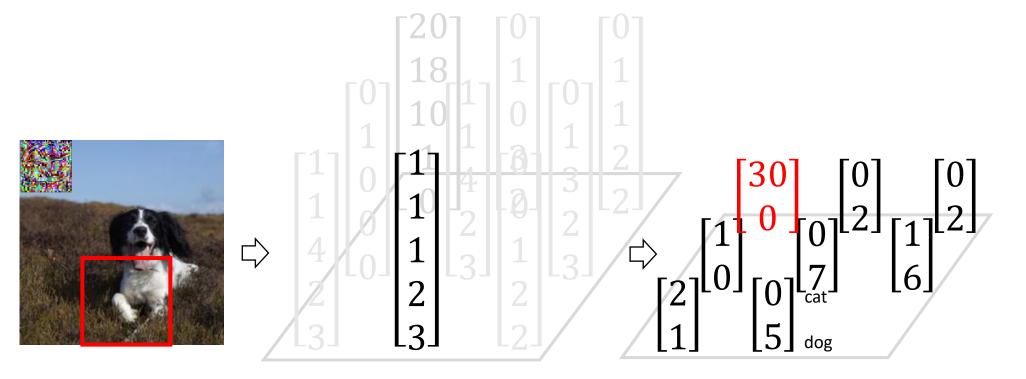
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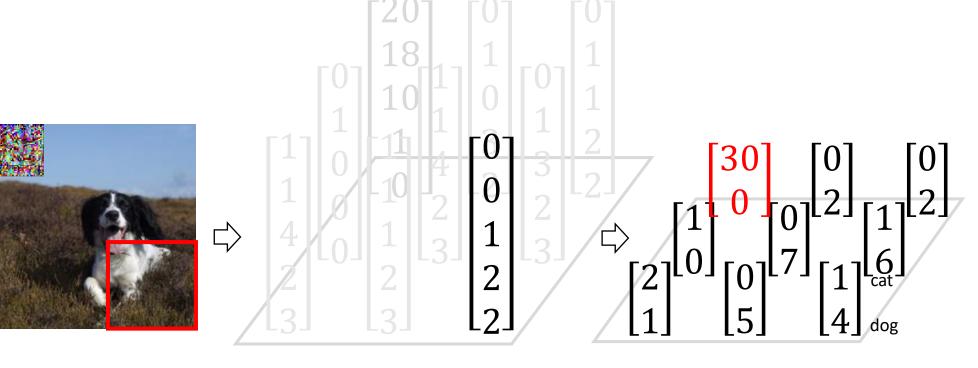
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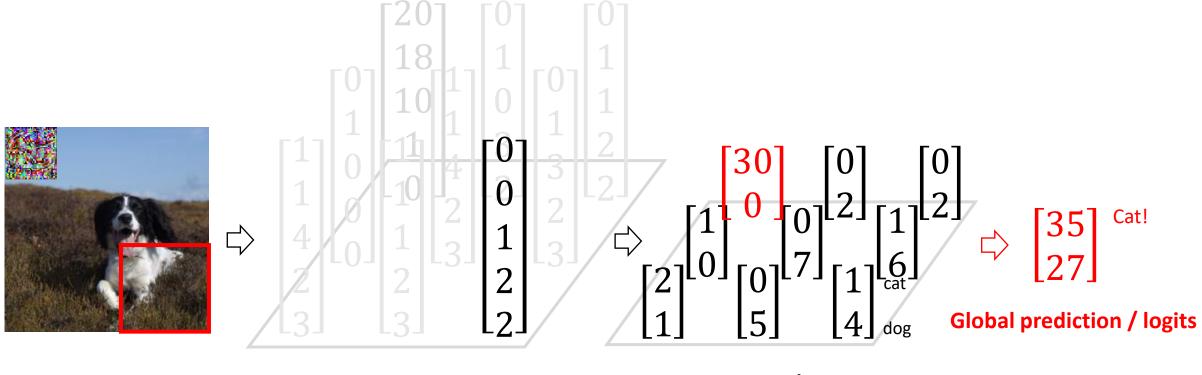
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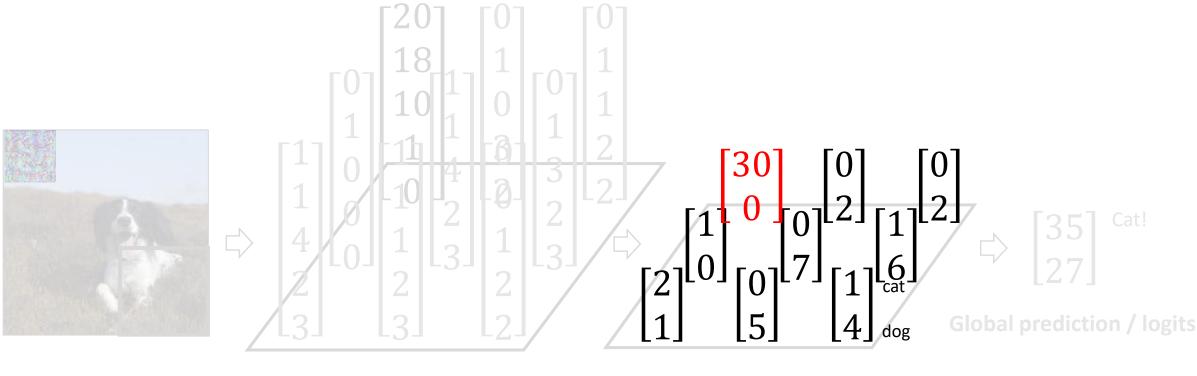
Aggregating local logits gives the same global logits prediction



Local feature map

Local prediction / logits map

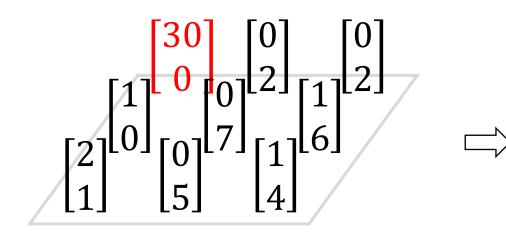
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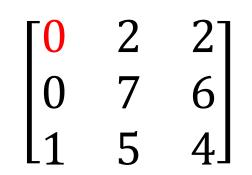
Local prediction / logits map

A Better Visualization: Local Logits Map Slice



 $\begin{bmatrix} 30 & 0 & 0 \\ 1 & 0 & 1 \\ 2 & 0 & 1 \end{bmatrix}$

local logits map slice for cat Cat: 35



local logits map slice for dog Dog: 27

- One local logits map slice for one class
- Class evidence: elements of each slice

Robust Masking: Algorithm

 $\begin{bmatrix}
 30 & 0 & 0 \\
 1 & 0 & 1 \\
 2 & 0 & 1
\end{bmatrix}$ local logits map slice for cat Cat: 35 local logits map slice for dog

Dog: 27

Robust Masking:

- 1. Clip all negative values to zeros
- 2. Move a <u>sliding window</u> over each local logits slice $(1 \times 1 \text{ window here})$
- 3. Calculate class evidence <u>sum</u> within each window
- 4. Mask the window with the highest sum

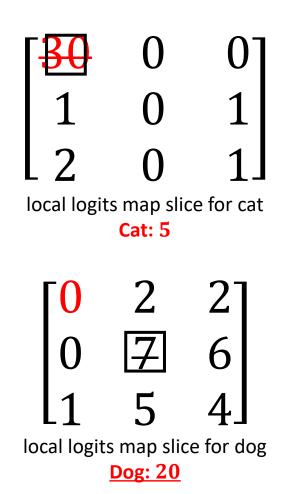
Robust Masking: Prediction in the Adversarial Setting

 $\begin{bmatrix}
 30 & 0 & 0 \\
 1 & 0 & 1 \\
 2 & 0 & 1
\end{bmatrix}$ local logits map slice for cat **Cat: 35** $\begin{bmatrix}
 0 & 2 & 2 \\
 0 & 7 & 6 \\
 1 & 5 & 4
\end{bmatrix}$ local logits map slice for dog

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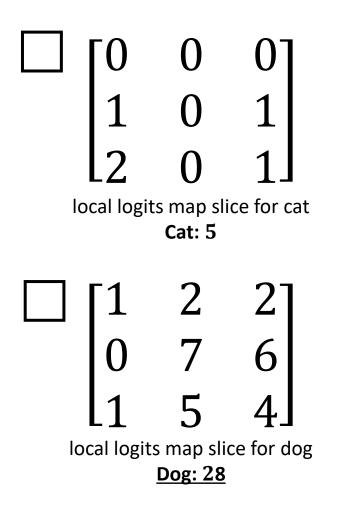


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The prediction in the adversarial setting is <u>subject to partial feature</u> <u>masking</u>

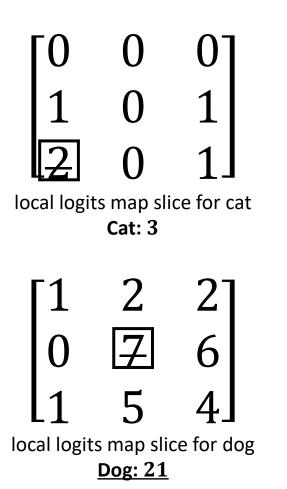
Robust Masking: Prediction in the Clean Setting



Robust Masking:

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Robust Masking: Prediction in the Clean Setting



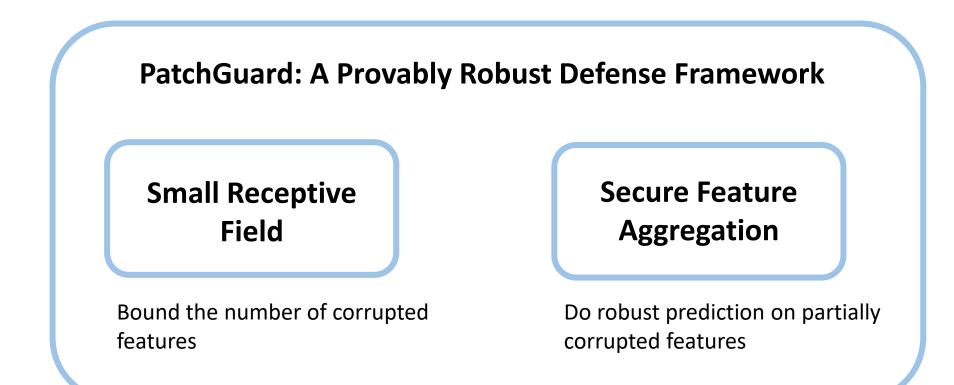
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- 3. Calculate class evidence <u>sum</u> within each window
- 4. Mask the window with the <u>highest</u> sum

The prediction in the clean setting is generally <u>invariant to partial feature</u> <u>masking</u>

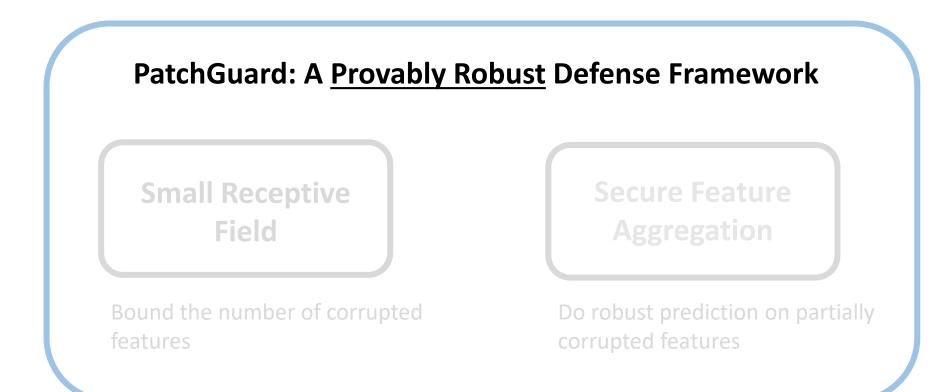
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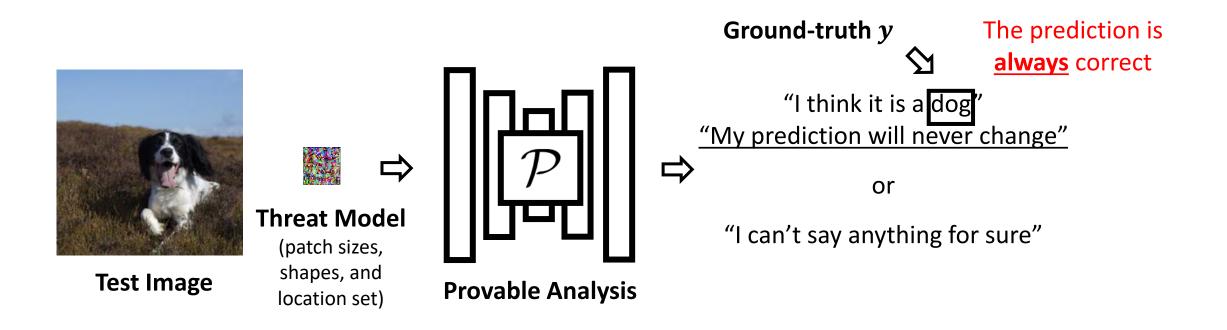


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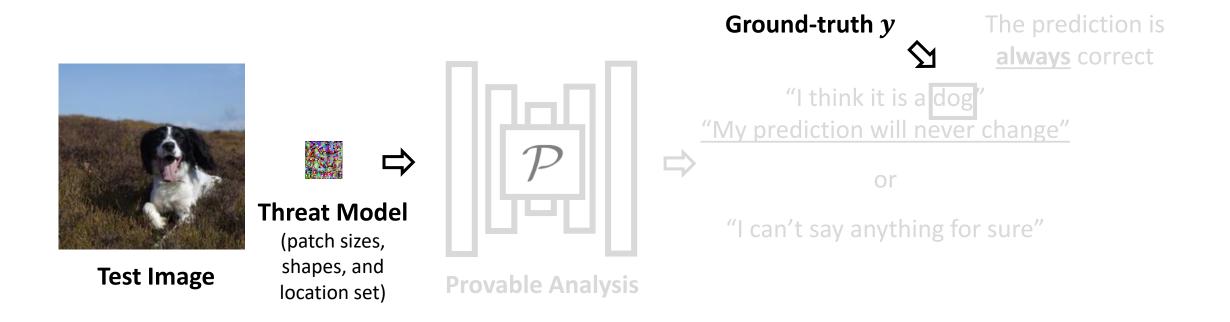
Recall: Provable Robustness on Certified Test Images



Provable robust accuracy / certified accuracy: the fraction of test images that are

- 1. Correctly classified
- 2. <u>Provably robust</u> to any (adaptive) localized patch attack within the threat model

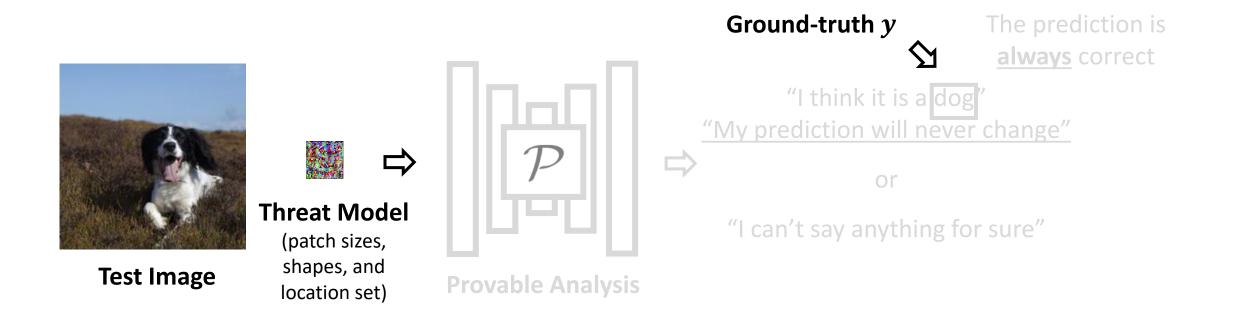
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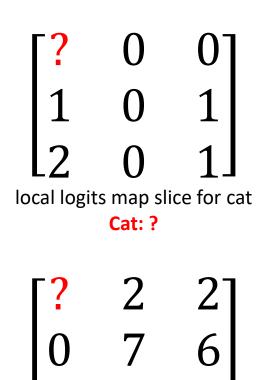
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Provable Analysis

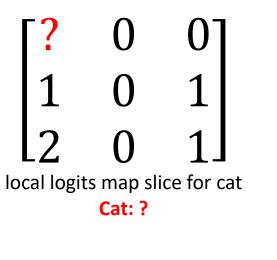


The adversary can control values within a small window (1 \times 1 window here)

local logits map slice for dog Dog: ?

5

Provable Analysis: Upper Bound of Class Evidence



The adversary can control values within a small window (1 \times 1 window here)

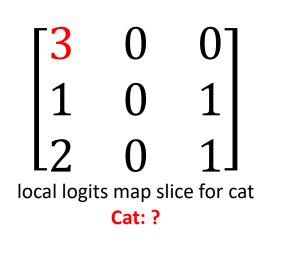
1. The adversary cannot increase the malicious class evidence too much

 $\begin{bmatrix} ? & 2 & 2 \\ 0 & 7 & 6 \\ 1 & 5 & 4 \end{bmatrix}$

local logits map slice for dog

Dog: ?

Provable Analysis: Upper Bound of Class Evidence



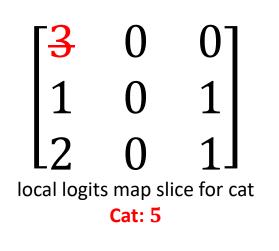
The adversary can control values within a small window $(1 \times 1 \text{ window here})$

- 1. The adversary cannot increase the malicious class evidence too much
 - A large value will be masked



local logits map slice for dog **Dog: ?**

Provable Analysis: Upper Bound of Class Evidence



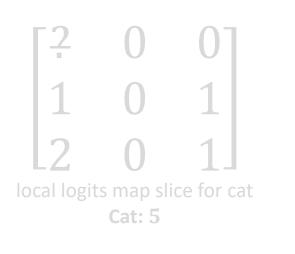
The adversary can control values within a small window (1 \times 1 window here)

- 1. The adversary cannot increase the malicious class evidence too much
 - A large value will be masked
 - The <u>robust masking</u> imposes an <u>upper bound</u> of the class evidence sum



local logits map slice for dog **Dog: ?**

Provable Analysis: Lower Bound of Class Evidence



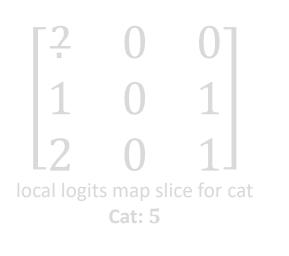
 $\begin{bmatrix} ? & 2 & 2 \\ 0 & 7 & 6 \\ 1 & 5 & 4 \end{bmatrix}$ local logits map slice for dog

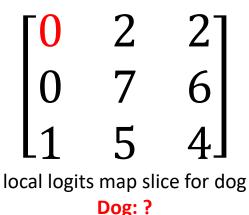
Dog: ?

The adversary can control values within a small window $(1 \times 1 \text{ window here})$

- 1. The adversary cannot increase the malicious class evidence too much
 - A large value will be masked
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- 2. The adversary cannot decrease the benign class evidence too much

Provable Analysis: Lower Bound of Class Evidence



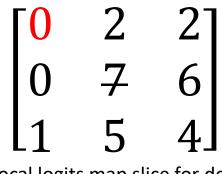


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- 2. The adversary cannot decrease the benign class evidence too much
 - Can only push malicious values to zero

Provable Analysis: Lower Bound of Class Evidence



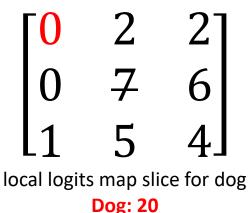


local logits map slice for dog Dog: 20 The adversary can control values within a small window $(1 \times 1 \text{ window here})$

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 - Can only push malicious values to zero
 - <u>Clipping all negative values</u> imposes a <u>lower bound</u> of the class evidence sum

Provable Analysis: Bounds hold for Any Attack Strategy



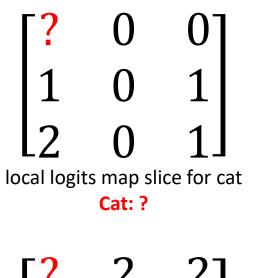


The adversary can control values within a small window (1×1 window here)

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- 2. The adversary cannot decrease the benign class evidence too much
 - Can only push malicious values to zero
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We can derive bounds that apply to any attack strategy! (formal proof in the paper)

Provable Analysis: Example



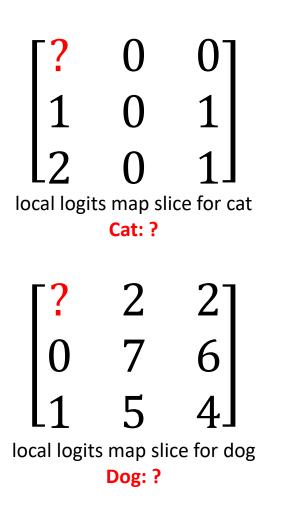
2	2]
7	2 6
5	4
	7

local logits map slice for dog

Dog: ?

	Lower Bound	Upper Bound
Cat	3	5
Dog	20	27

Provable Analysis: Example



	Lower Bound	Upper Bound
Cat	3	5
Dog	20	27

- 20 (lower bound of dog) > 5 (upper bound of cat)
 - Provably Robust (always predicts dog)!
- Try all possible patch locations
 - This image is certified :)





Threat Model (patch sizes, shapes, and location set)

Test Image

Evaluation: Substantial Provable Robustness

	10-class ImageNette		
Accuracy	Clean Robust		
PatchGuard	95.0%	86.7%	

1. PatchGuard achieves substantial provable robustness

(robustness evaluated against a 2%-pixel square patch *anywhere* on the image)

Evaluation: Substantial Provable Robustness

	10-class ImageNette		1000-class	ImageNet
Accuracy	Clean	Robust	Clean	Robust
PatchGuard	95.0%	86.7%	54.6%	26%

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Evaluation: Substantial Provable Robustness

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Accuracy	Clean	Robust	Clean	Robust		
PatchGuard	95.0%	86.7%	54.6%	26%		
PatchGuard- Top-5			76.6%	56.9%		

Top-5 accuracy for ImageNet is good!

1. PatchGuard achieves substantial provable robustness

(robustness evaluated against a 2%-pixel square patch *anywhere* on the image)

Evaluation: State-of-the-art Clean Accuracy and Provable Robust Accuracy

	10-class ImageNette		1000-class	ImageNet
Accuracy	Clean	Robust	Clean	Robust
PatchGuard	95.0%	86.7%	54.6%	26%
IBP [1]	Computationally infeasible			
CBN [2]	94.9%	60.9%	49.5%	7.1%
DS [3]	92.1%	79.1%	44.4%	14.4%

2. IBP is too computationally expensive to scale to high-resolution images

- 3. PatchGuard significantly outperforms CBN and DS
 - Improvement from CBN on ImageNet:
 - 5% clean accuracy; 19% provable robust accuracy (2x better!)
 - Improvement from DS on ImageNet:
 - 10% clean accuracy; 12% provable robust accuracy (1x better!)

[1] Chiang et al., "Certified Defenses for Adversarial Patches," ICLR 2020

[2] Zhang et al., "Clipped bagnet: Defending against sticker attacks with clipped bag-of-features," DLS Workshop 2020

[3] Levine et al., "(De)randomized smoothing for certifiable defense against patch attacks," NeurIPS 2020

Discussion: Generalizability of PatchGuard

PatchGuard as a general defense framework

Provably Robust Defense	Small receptive field	Secure feature aggregation
PatchGuard (ours)	BagNet	Robust masking

Discussion: Generalizability of PatchGuard

PatchGuard as a general defense framework

Provably Robust Defense	Small receptive field	Secure feature aggregation
PatchGuard (ours)	BagNet	Robust masking
Clipped BagNet (CBN) [1]	BagNet	Clipping + Average pooling
Derandomized Smoothing (DS) [2]	Pixel patches to ResNet	Majority voting

Discussion: Generalizability of PatchGuard

PatchGuard as a general defense framework

Provably Robust Defense	Small receptive field	Secure feature aggregation
PatchGuard (ours)	BagNet	Robust masking
Clipped BagNet (CBN) [1]	BagNet	Clipping + Average pooling
Derandomized Smoothing (DS) [2]	S) [2] Pixel patches to ResNet Majority voting	
BagCert [3]	Modified BagNet	Majority voting
Randomized Cropping [4]	Cropped images to ResNet	Majority voting

[1] Zhang et al., "Clipped bagnet: Defending against sticker attacks with clipped bag-of-features," DLS Workshop 2020

[2] Levine et al., "(De)randomized smoothing for certifiable defense against patch attacks," NeurIPS 2020

[3] Metzen et al., "Efficient certified defenses against patch attacks on image classifiers," ICLR 2021

[4] Lin et al. "Certified robustness against physically-realizable patch attack via randomized cropping," ICLR Open Review 2021

Discussion: Limitations

- 1. The small receptive field hurts the clean accuracy (provable robustness vs. clean accuracy trade-off)
 - The accuracy drop is especially obvious for ImageNet (from 76.1% to 56.5%)

	10-class ImageNette		1000-class	ImageNet
	Clean	Robust	Clean	Robust
ResNet-50 (483 × 483)	99.6%		76.1%	
BagNet-17 (17 × 17)	95.9%		56.5%	
PatchGuard	95.0%	86.7%	54.6%	26%
PatchGuard- Top-5			76.6%	56.9%

2. The masking operation requires additional parameters (e.g., number of masks, mask size, mask shape)

Takeaways

1. PatchGuard: a General Defense Framework

- Small receptive field
- Secure feature aggregation

2. Provably Robust Defense

• Predictions are always correct on certified images

3. State-of-the-art Defense Performance

- Clean accuracy
- Provable robust accuracy

Thank you!

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Technical Report

<u>GitHub</u>